

Rossmoyne Senior High School



Semester One Examination, 2018

Question/Answer booklet

MATHEMATICS SPECIALIST UNIT 3

Section One:
Calculator-free

If required by your examination administrator, please
place your student identification label in this box

Student number: In figures

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In words

Your name

Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	53	35
Section Two: Calculator-assumed	13	13	100	97	65
				Total	100

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you do not use pencil, except in diagrams.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section One: Calculator-free

35% (53 Marks)

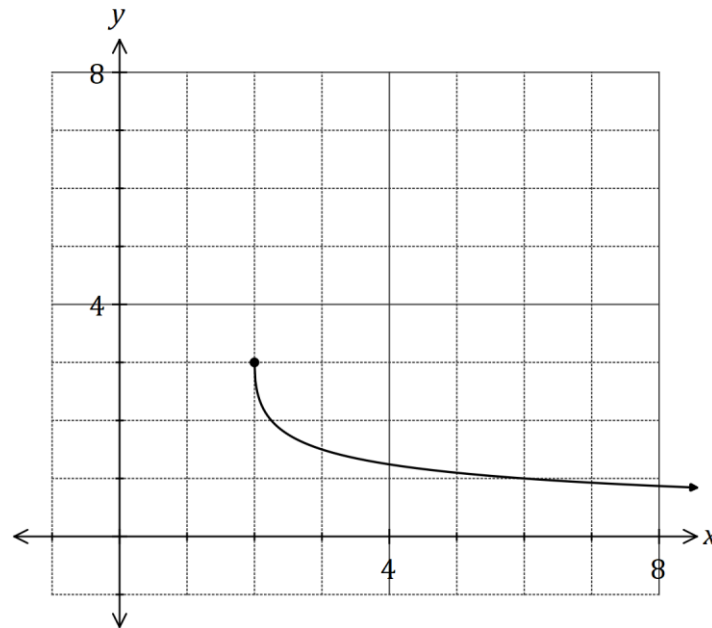
This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1

(6 marks)

The graph of $y = f(x)$ is shown below, where $f(x) = \frac{3}{1 + \sqrt{x - 2}}$.



- (a) Sketch the graph of $y = f^{-1}(x)$ on the same axes. (2 marks)
- (b) Determine the defining rule for $y = f^{-1}(x)$ and state its domain. (4 marks)

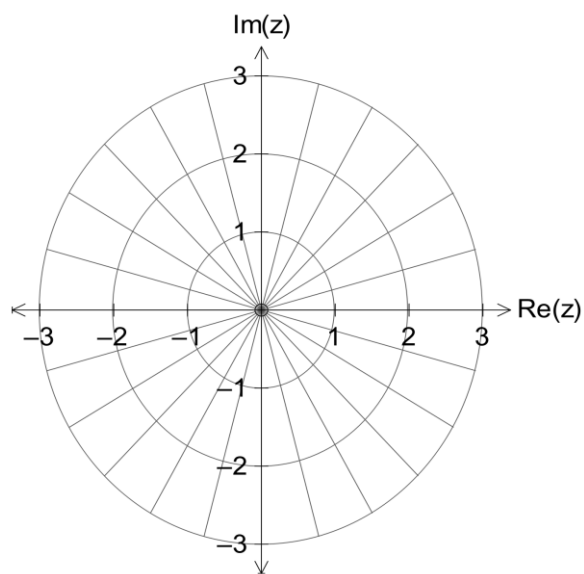
Question 2

(7 marks)

The solutions to the equation $z^3 - w = 0$ are of the form $z = r \operatorname{cis} \theta$, where $z, w \in \mathbb{C}$, $r > 0$ and $-\pi < \theta \leq \pi$. One of the solutions is $z = 3 \operatorname{cis} \left(-\frac{\pi}{2}\right)$.

(a) Determine the complex number w in polar form. (2 marks)

(b) Sketch all solutions on the polar grid provided below. (2 marks)



(c) The solutions form the outline of a regular shape. Determine the exact perimeter of this regular shape. (3 marks)

Question 3**(7 marks)**

Consider $f(z) = 3z^3 + 2z^2 + 15z + 10$, where z is a complex number.

(a) Determine, with reasons, which of the following are factors of $f(z)$.

(i) $z + 2$.

(2 marks)

(ii) $z - \sqrt{5}i$.

(2 marks)

(b) Solve the equation $f(z) = 0$.

(3 marks)

Question 4

(10 marks)

The points A , B and C have position vectors $(1, 0, -2)$, $(p, -2, 1)$ and $(2, -1, 0)$ respectively.

- (a) Determine the **vector** equation for the line through A and C , in the form $\mathbf{r} = \mathbf{a} + \lambda\mathbf{b}$.
(2 marks)

- (b) Determine, in terms of p , the **Cartesian** equation of the plane containing A , B and C .
(5 marks)

- (c) The line with equation $\mathbf{r} = (3, -5, 6) + \mu(2, q, -12)$ is **perpendicular** to the plane containing A , B and C . Determine the values of the constants p and q .
(3 marks)

Question 5**(6 marks)**

(a) Solve this system of equations.

(3 marks)

$$\begin{aligned}x + y + 2z &= 1 \\4x + y - z &= 7 \\3x - y + z &= 14\end{aligned}$$

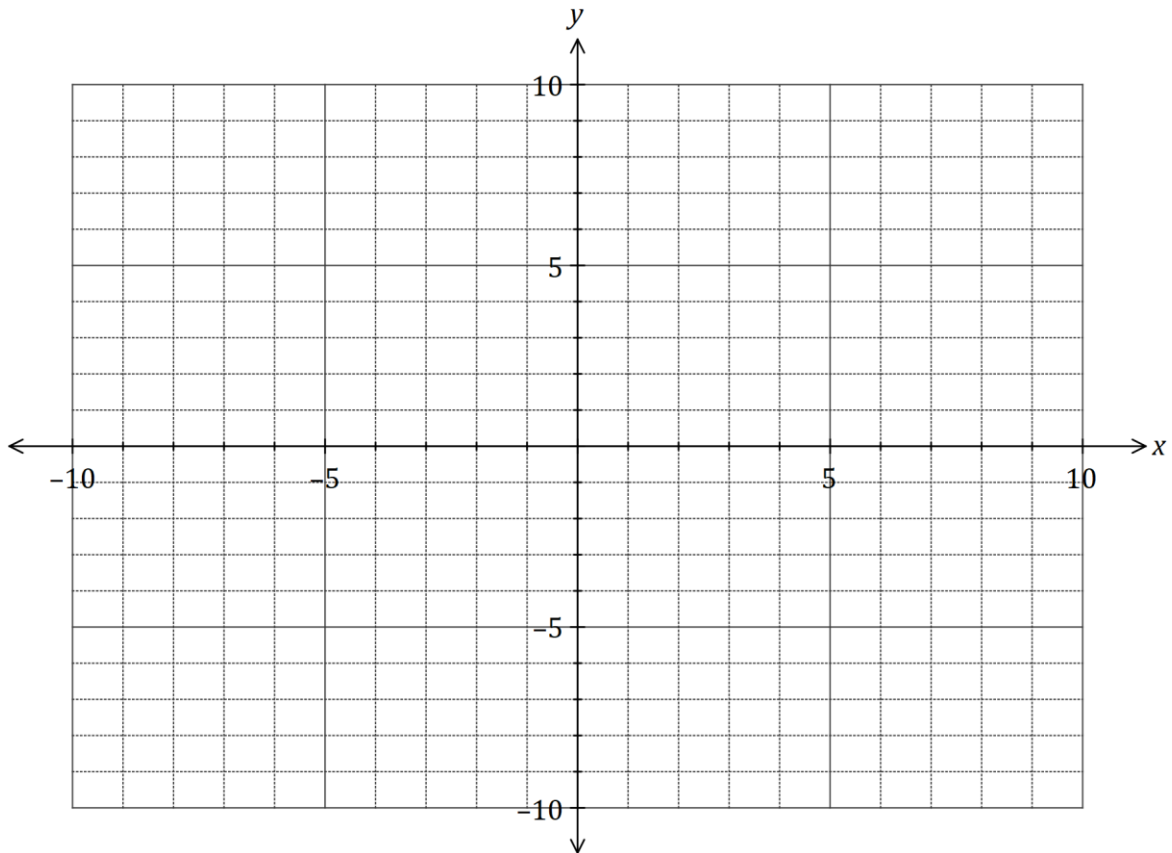
(b) Determine the value of constant a so that the following system of equations does not have a unique solution and give a brief geometric interpretation of the system of equations with this value. **(3 marks)**

$$\begin{aligned}x + y + 2z &= 1 \\4x + y - z &= 7 \\ax - y + z &= 14\end{aligned}$$

Question 6

(6 marks)

The graph of $y = \frac{(x + 4)(x - 4)}{x^2 - 4x - 5}$ has no stationary points. Sketch the graph.



Question 7**(5 marks)**

The complex numbers u and w satisfy the equations $u - w = 6i$ and $uw = 13$.

Solve the equations for u and w , giving your solution(s) in the form $a + bi$, where a and b are real.

Question 8

(6 marks)

A function is defined by $g(x) = \frac{5-x}{(5x+8)(2x-3)}$.

(a) State the natural domain of $f(x)$. (1 mark)

(b) State the **equations** of all asymptotes of the graph of $y = x \cdot f(x)$. (2 marks)

(c) The graph of $y = \frac{1}{f(x)}$ has an asymptote with equation $y = ax + b$. Determine the values of the constants a and b . (3 marks)

Supplementary page

Question number: _____

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